# Resonance Interactions in Acyclic Systems. 2. Y-Conjugated Anions and Cations 

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#### Abstract

The first and second ionization energies of isobutene, acetone, acetic acid, and carbonic acid were calculated at the MP3/6-311++G**//6-31G* level giving values that agreed with the available experimental data. The first ionization energy decreased by $21 \mathrm{kcal} / \mathrm{mol}$ for each of the first two replacements of $\mathrm{CH}_{2}$ by O but decreased by only $10 \mathrm{kcal} / \mathrm{mol}$ for the third replacement. The second ionization energy was high and was the same for the first three compounds. It decreased for the third replacement of $\mathrm{CH}_{2}$ by O . It was concluded that the electronegativity of the terminal atoms determines the ionization energies, and that there was no evidence for Y aromaticity in the gas phase. In solution, the anions formed ion pairs or triplets with lithium, and this markedly reduced the energies of formation. The energies of reaction of isobutene with lithium hydride were calculated, and both the first and second reactions were found to be exothermic. The cations formed by the loss of one or two hydride ions from isobutene, and by the addition of a proton to guanidine, also were studied. The allyl cations had significant resonance stabilization, but no special stabilization was found for the dication. Guanidinium ion was found to have little if any resonance stabilization. The origin of the basicity of guanidine is discussed.


One of the remarkable observations in carbanion chemistry is the facile reaction of butyllithium with the monoanion derived from isobutene to give the dianion. ${ }^{1}$ This and related observations have received considerable attention and have been attributed either to "Y-aromaticity" 2.3 or to internal coulombic stabilization resulting from charge alternation. ${ }^{4}$ Both viewpoints have recently been reviewed. ${ }^{3.4}$

In our study of the formation of allyl anions from their neutral precursors, we found it useful to examine the effect on the ionization energy of replacing the terminal carbons by NH or $\mathrm{O} .^{5}$ Here, it was found that the replacement of one $\mathrm{CH}_{2}$ by NH reduced the ionization energy by $12 \mathrm{kcal} / \mathrm{mol}$, and replacement of one $\mathrm{CH}_{2}$ by O reduced the ionization energy by $23 \mathrm{kcal} / \mathrm{mol}$. Further, the effects were additive.

We have now examined the replacement of carbons in isobutene and the allyl anions ${ }^{6}$ derived from it by oxygen. In each case, the geometry was optimized with use of the $6-31 G^{*}$ basis set, ${ }^{7}$ and then the MP3/6-311++G** energy was obtained at that geometry. This flexible basis set, which is effectively triple- $\zeta$ and includes both diffuse and polarization functions at all atoms, was found to give ionization energies in good accord with the experimental data for the allyl anions. ${ }^{5}$ The energies are given in Table 1, and the structural parameters are given in Table II. In the case of methallyl anion, two rotamers of the methyl group were examined (1a and 1b) and were found to have essentially the same energy.

The ionization energies, which may be obtained from the data in Table I, are summarized in Table III. There was a considerable change in calculated ionization energies on going from 6-31G* to $6-311++G^{* *}$ showing the necessity of using a flexible basis set in studying these reactions. The MP2 correction for electron correlation overcorrected as is often found to be the case. ${ }^{8}$ The

[^0]MP3 values were close to RHF, and in the earlier related study, the MP4 correction had only a small effect. ${ }^{5}$ It was not calculated in the present case because of the size of some of the systems being studied. In order to compare the calculated values with experimental data, ${ }^{9}$ it was necessary to correct them for the loss of zero-point energy on ionization, corresponding to the loss of one $\mathrm{X}-\mathrm{H}$ stretching mode and two $\mathrm{X}-\mathrm{H}$ bending modes, where X is C or O . The zero-point energy changes were assumed to be the same as for the closely related systems we studied previously, ${ }^{5}$ leading to the calculated $\Delta H$ values in the table. They are in quite good agreement with experiment.

It is easier to visualize the results by an examination of Figure 1, which shows the ionization energies as a function of the number of oxygens. It can be seen that the first ionization energy changed by $21 \mathrm{kcal} / \mathrm{mol}$ for each of the first two replacements of C by O , but that the third replacement decreased the energy by only 10 $\mathrm{kcal} / \mathrm{mol}$. In the second ionization step, the first two replacements of C by O had no effect on the ionization energy, but the third replacement decreased the energy by $16 \mathrm{kcal} / \mathrm{mol}$.

These energy changes may readily be understood by examining the ions that are formed. The first ionization step gives the following ions:


Here, the first three ions are related by replacing a carbon in an allyl anion by oxygen, and as noted previously, the electronegativity of oxygen results in a reduced relative energy. However, with the last ion, the only effect is derived from the replacement of a nonreacting $\mathrm{CH}_{3}$ by a nonreacting OH . It is not surprising that this gives a smaller effect on the ionization energy.

The ions formed in the second ionization step are


2


4


6


8

The first three ions are formed by removing a proton from a methyl group, and the energy change is independent of the rest of the

[^1]Table I. Energies of Anions Formed by Proton Loss, H

| compd | 6.31G* | $6-311++\mathrm{G}^{* *}(6 \mathrm{D})$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | RHF | RHF | MP2 | MP3 |
| isobutene | -156.11067 | -156.15337 | -156.75250 | -156.79463 |
| methallyl anion 1a ${ }^{\text {a }}$ | -155.43085 | -155.50010 | -156.11452 | -156.14776 |
| methallyl anion $\mathbf{1 b}^{\text {b }}$ | -155.43078 | -155.50003 | -156.11430 | -156.14755 |
| trimethylenemethyl dianion 2 | -154.54723 | -154.67236 | -155.30020 | -155.32382 |
|  | -191.96223 | -192.01751 | -192.66224 | -192.68670 |
| enolate anion 6 | -191.32303 | -191.39783 | -192.05658 | -192.07216 |
| enolate dianion 4 | -190.44506 | -190.57334 | -191.24498 | -191.25117 |
| acetic acid | -227.81065 | -227.88384 | -228.57685 | -228.57400 |
| acetate anion 5 | -227.22506 | -227.30007 | -228.01106 | -228.009 19 |
| acetate dianion 6 | -226.34994 | -226.48224 | -227.19816 | -227.18689 |
| carbonic acid | -263.64748 | -263.738 38 | -264.477 77 | -264.46974 |
| bicarbonate anion 7 | -263.07861 | -263.17901 | -263.92762 | -263.91084 |
| carbonate dianion 8 | -262.25060 | -262.38569 | -263.143 42 | -263.11618 |

${ }^{a}$ One methyl hydrogen perpendicular to the plane of the carbon atoms. ${ }^{b}$ One methyl hydrogen in the plane of the carbon atoms.

Table II. Calculated Structures, $6-31 G^{* a}$

| compd | unit | value |
| :---: | :---: | :---: |
| isobutene | $r(\mathrm{C}=\mathrm{C})$ | 1.321 |
|  | $r(\mathrm{C}-\mathrm{C})$ | 1.508 |
|  | $\angle \mathrm{C}_{1} \mathrm{C}_{2} \mathrm{C}_{3}$ | 122.3 |
| methallyl anion 1a | $r\left(\mathrm{C}_{1}-\mathrm{C}_{2}\right)$ | 1.530 |
|  | $r\left(\mathrm{C}_{2}-\mathrm{C}_{3}\right)$ | 1.384 |
|  | $\angle \mathrm{C}_{1} \mathrm{C}_{2} \mathrm{C}_{3}$ | 115.1 |
| methallyl anion 1b | $r\left(\mathrm{C}_{1}-\mathrm{C}_{2}\right)$ | 1.529 |
|  | $r\left(\mathrm{C}_{2}-\mathrm{C}_{3}\right)$ | 1.385 |
|  | $r\left(\mathrm{C}_{2}-\mathrm{C}_{4}\right)$ | 1.382 |
|  | $\angle \mathrm{C}_{1} \mathrm{C}_{2} \mathrm{C}_{3}$ | 114.9 |
|  | $\angle \mathrm{C}_{1} \mathrm{C}_{2} \mathrm{C}_{4}$ | 115.2 |
| methallyl dianion 2 | $r(\mathrm{C}-\mathrm{C})$ | 1.431 |
|  | $\angle \mathrm{CCC}$ | 120.0 |
| acetone | $r(\mathrm{C}=\mathrm{O})$ | 1.192 |
|  | $r(\mathrm{C}-\mathrm{C})$ | 1.513 |
|  | $\angle O C C$ | 121.7 |
| etnolate anion 3 | $r(\mathrm{C}-\mathrm{O})$ | 1.252 |
|  | $r\left(\mathrm{C}_{2}-\mathrm{C}_{3}\right)$ | 1.371 |
|  | $r\left(\mathrm{C}_{3}-\mathrm{C}_{4}\right)$ | 1.552 |
|  | $\mathrm{LOC}_{3} \mathrm{C}_{2}$ | 128.7 |
|  | $L^{(O C} C_{3}$ | 115.5 |
| enolate dianion 4 | $r(\mathrm{C}-\mathrm{O})$ | 1.291 |
|  | $r(\mathrm{C}-\mathrm{C})$ | 1.433 |
|  | $\angle O C C$ | 119.6 |
| acetic acid | $r(\mathrm{C}=\mathrm{O})$ | 1.187 |
|  | $r(\mathrm{C}-\mathrm{O})$ | 1.332 |
|  | $r(\mathrm{C}-\mathrm{C})$ | 1.502 |
|  | $\angle O C C$ | 125.8 |
|  | $\angle O C O$ | 122.4 |
| acetate anion 5 | $r(\mathrm{C}-\mathrm{C})$ | 1.554 |
|  | $r\left(\mathrm{C}-\mathrm{O}_{1}\right)$ | 1.233 |
|  | $r\left(\mathrm{C}-\mathrm{O}_{2}\right)$ | 1.235 |
|  | $\angle \mathrm{CCO}_{1}$ | 116.0 |
|  | $\angle \mathrm{CCO}_{2}$ | 114.5 |
| acetate dianion 6 | $r(\mathrm{C}-\mathrm{O})$ | 1.283 |
|  | $r(\mathrm{C}-\mathrm{C})$ | 1.437 |
|  | $\angle \mathrm{C}-\mathrm{C}-\mathrm{O}$ | 121.4 |
| carbonic acid | $r(\mathrm{C}=\mathrm{C})$ | 1.188 |
|  | $r(\mathrm{C}-\mathrm{O})$ | 1.315 |
|  | $\angle \mathrm{O}=\mathrm{CO}$ | 125.1 |
| bicarbonate 7 | $r\left(\mathrm{C}-\mathrm{O}_{1}\right)$ | 1.224 |
|  | $r\left(\mathrm{C}-\mathrm{O}_{2}\right)$ | 1.219 |
|  | $r\left(\mathrm{C}-\mathrm{O}_{3}\right)$ | 1.401 |
|  | $\angle \mathrm{O}_{1} \mathrm{CO}_{2}$ | 132.0 |
|  | $\angle \mathrm{O}_{1} \mathrm{CO}_{3}$ | 113.5 |
| carbonate 8 | $r(\mathrm{C}-\mathrm{O})$ | 1.285 |
|  | $\angle O C O$ | 120.0 |

${ }^{a}$ The lengths are given in $\AA$ and the angles in deg. The numbering of the atoms is shown in Table V .
molecule. However, in the formation of carbonate ion, the proton is removed from oxygen, and consequently the ionization energy is reduced.

It can be seen that the energy changes are determined solely by the electronegativity of the groups at the terminal positions,


Figure 1. Lonization energies as a function of the number of terminal oxygens. The lower line is for the first ionization step, and the upper line is for the second step.
and there is no need to postulate resonance stabilization. This is in good accord with conclusions that have been reached for allyl anions. ${ }^{5}$ For example, with carboxylic acids, the ionization process might best be written as ${ }^{10}$


This would be in accord with the very small change in electron population at the oxygens as a result of ionization and the strong polarization of carbonyl groups. As might be expected the second ionization energies were considerably larger than the first, as has been observed in solution with carbonic acid (first $\mathrm{p} K_{\mathrm{a}}=3.7$, second $\mathrm{p} K_{\mathrm{a}}=10.3$ ). ${ }^{11}$

In view of these results, how does one rationalize the experimental observation of the ease of forming the dianion from isobutene? Theoretical studies by Streitwieser et al. ${ }^{12}$ and by Schleyer

[^2]Table III. Energy Changes on lonization ( $\mathrm{kcal} / \mathrm{mol}$ )

| reaction | 6-31G* | $6-311++\mathrm{G}^{* *}(6 \mathrm{D})$ |  |  | $\Delta H$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RHF | RHF | MP2 | MP2 | est ${ }^{\text {a }}$ | obs |
| isobutene $\rightarrow$ anion | 426.6 | 409.9 | 400.3 | 405.9 | 395 | $397 \pm 3$ |
| anion $\rightarrow$ dianion | 554.5 | 519.4 | 511.0 | 517.0 |  |  |
| acetone $\rightarrow$ anion | 401.1 | 388.8 | 380.1 | 385.6 | 375 | $369 \pm 3$ |
| anion $\rightarrow$ dianion | 550.9 | 517.4 | 509.3 | 515.2 |  |  |
| acetic acid $\rightarrow$ anion | 367.5 | 361.3 | 355.0 | 360.7 | 352 | $349 \pm 3$ |
| anion $\rightarrow$ dianion | 549.1 | 518.2 | 510.1 | 516.0 |  |  |
| carbonic $\rightarrow$ bicarbonate | 357.0 | 351.0 | 345.2 | 350.7 | 342 |  |
| bicarbonate $\rightarrow$ carbonate | 519.6 | 497.8 | 492.1 | 498.6 |  |  |

${ }^{a}$ Derived from the MP3/6-311++G** energies by correction for zero-point energy differences ( $11 \mathrm{kcal} / \mathrm{mol}$ for cleavage of a CH bond and 9 $\mathrm{kcal} / \mathrm{mol}$ for the cleavage of an OH bond).

Table IV. Energies of Lithio Derivatives
(a) Total Energies, H

| compd | 6-31G* | $6.311 \mathrm{G}^{* *}(6 \mathrm{D})$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | RHF | RHF | MP2 | MP3 |
| isobutene | -156.11067 | -156.15183 | -156.74940 | -156.79174 |
| 2-methylallyllithium | -162.955 22 | -162.99928 | -163.61094 | -163.64625 |
| dilithioisobutene | -169.80211 | -169.848 32 | -170.47380 | -170.50267 |
| lithium hydride | -7.98087 | -7.98586 | -8.00871 | -8.01422 |
| hydrogen | -1.12683 | -1.13152 | -1.15915 | -1.16501 |

(b) Energy Changes, kcal/mol

| reaction | $6.31 \mathrm{G}^{*}$ | 6-311 ${ }^{* *}$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | RHF | RHF | MP2 | MP3 |
| isobutene $+\mathrm{LiH} \rightarrow 2$-methylallyllithium $+\mathrm{H}_{2}$ | +6.0 | +4.3 | -7.5 | -3.3 |
| 2-methylallyllithium $+\mathrm{LiH} \rightarrow$ dilithio $+\mathrm{H}_{2}$ | +6.8 | +3.3 | -8.3 | -4.5 |

et al. ${ }^{13}$ have shown that dilithiopropene and related compounds adopt bridged structures that maximize coulombic attraction between the lithium cations and the anion. It appeared likely that the same would be true with dilithioisobutene. The geometries of the monolithio and dilithio derivatives of isobutene were optimized with use of the $6-31 \mathrm{G}^{*}$ basis set, and the energies were calculated at the MP3/6-311G** level. The structures are shown in Figure 2, and the energies are given in Table IV. They were shown to be true minima by calculating the vibrational frequencies at the $6-31 \mathrm{G}^{*}$ level. No imaginary frequencies were found. The lowest calculated frequencies were $132 \mathrm{~cm}^{-1}$ for the monolithio compound and $159 \mathrm{~cm}^{-1}$ for the dilithio compound.

The energy changes for the following reactions were calculated with these data:

$$
\begin{aligned}
& \left(\mathrm{CH}_{3}\right)_{2} \mathrm{C}=\mathrm{CH}_{2}+\mathrm{LiH} \rightarrow \mathrm{CH}_{3} \mathrm{C}\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{Li}^{+}+\mathrm{H}_{2} \\
& \mathrm{CH}_{3} \mathrm{C}\left(\mathrm{CH}_{2}\right)_{2}{ }^{-} \mathrm{Li}^{+}+\mathrm{LiH} \rightarrow \mathrm{C}\left(\mathrm{CH}_{2}\right)_{3}{ }^{2-} 2 \mathrm{Li}^{+}+\mathrm{H}_{2}
\end{aligned}
$$

The calculated energy changes were significantly affected by the correction for electron correlation, and with the MP3/6-311G** energies, the first reaction was calculated to have $\Delta E=-3.3$ $\mathrm{kcal} / \mathrm{mol}$ and the second to have $\Delta E=-4.5 \mathrm{kcal} / \mathrm{mol}$. The two energy changes were exothermic and were now very close. This accounts for the observed ease of formation of the dilithio compound. The structures (Figure 2) were those that will maximize the coulombic attraction of the lithium cation(s) for the anions. It seems clear that the formation of the dilithio compounds has little if anything to do with " Y -aromaticity".

Charge Distribution. On the basis of the charge distribution derived from the Mulliken population analysis, it has been suggested that the isobutene dianion is stabilized by an attractive coulombic interaction between the central carbon with a positive charge and the terminal carbons bearing a negative charge. ${ }^{4}$ However, Both Mulliken ${ }^{14}$ and others ${ }^{15}$ have noted the deficiency

[^3]

Figure 2. Structures of lithio derivatives of isobutene: (a) the monolithio derivative; (b) the dilithio derivative. The lithiums are shown shaded.
in the population analysis which uses an arbitrary division of charge density between atoms and is basis set dependent.

This is well illustrated by the central carbon atom of isobutene. The use of the $6-31 \mathrm{G}^{*}$ basis set led to a Mulliken population of 5.892 e , corresponding to a charge of +0.108 . With the larger basis set, the population decreased to 4.989 e , corresponding to

[^4]




Figure 3. Atomic charges and energies derived via numerical integration for the anions and their parents. The first value ( $T$ ) is the total charge, the second $(\pi)$ is the charge for the $\pi$ system, and the third is the kinetic energy. which is minus the total energy for the group or atom. In the case of methallyl anion, conformer 1 lb is shown.
a charge of $1.011!$ Neither charge is reasonable. An $\mathrm{sp}^{2}$ hybridized carbon is more electronegative than an $\mathrm{sp}^{3}$ hybridized carbon, and so there should be a drift of charge density from the methyl group to the central carbon, and it should have a small negative charge.

A more satisfactory procedure makes use of Bader's theory of atoms in molecules. ${ }^{16}$ Here, zero-flux surfaces are located which separate pairs of bonded atoms. The collection of these surfaces will serve to separate a molecule into a set of atomic domains. Integration of the charge density within one of these domains gives the electron population for the given atom, and similarly, integration of the kinetic energy gives the atomic kinetic energy ( $T_{\Omega}$ ) that is directly related to the total energy of the atoms $\left(E_{\Omega}=-T_{\Omega}\right)$.

The results of this analysis for the anions are given in Table V. As expected, the electron population at the central carbon of isobutene was 6.050 e , corresponding to a charge of -0.050 . The total population for the methyl group was 8.963 e , leading to a small positive charge, +0.037 . The group charges for the anions and their parents are summarized in Figure 3.

The monoanion of isobutene again had a small negative charge at the central carbon, and most of the negative charge was at the methylene groups (av-0.422). However, some of the negative charge appeared at the methyl group ( -0.113 ). Finally, with the dianion, the central carbon had only a small positive charge $(+0.040)$ and the methylene groups bore essentially $2 / 3$ of a negative charge each ( -0.679 ). These results do not support the idea of internal coulombic stabilization. It is interesting to note that the hydrogens bore a considerable part of the negative charge in the anions. This is in accord with simple electrostatic concepts, in which an ion will try to put the charge on as large a volume element as possible in order to reduce the electrostatic energy.

In the case of acetone, the carbonyl group was strongly polarized $\mathrm{C}^{+}-\mathrm{O}^{-}$as is usually found with this group. ${ }^{17}$ The charge resulted from two factors, both related to the difference in electronegativity between carbon and oxygen. The more electronegative oxygen

[^5]will cause some shift in charge density from the carbon to the oxygen. This will, in turn, cause the bond critical point to move toward the carbon. The zero-flux surfaces pass through the critical point, and as a result the "size" of the oxygen in the direction of the carbon increases. The combination of the charge shift and the increased size leads to the relatively large charges assigned to carbon and oxygen.
Turning to the anions derived from acetone (Figure 3), it can be seen that the charge at the terminal carbon was not much different than that found for the isobutene derived ions. However, it was adjacent to a more electron deficient carbon, resulting in greater internal coulombic stabilization. The deprotonation of acetate ion again led to charges in the terminal carbon that were similar to those for the dianions derived from isobutene and acetone, and the increased stabilization of acetate was in part a result of the greater electron deficiency at the central carbon. It can be seen that the internal coulombic stabilization originally proposed for the isobutene dianion is actually found in the anions derived from acetone and acetic acid.

The $\pi$-electron populations for each of the atomic regions also are given in Table V and Figure 3. Some polarization of the $\pi$-charge is seen with the trimethylenemethyl dianion where the central carbon has a small positive $\pi$-charge. It should be noted that whereas the full atomic charges are well defined as the atomic number less the calculated electron population, the $\pi$-charges are formal charges based on "normal" populations of 2 for each $\mathrm{CH}_{3}$ or OH group and 1 for each atom involved with a double bond. The large change in $\pi$-charge for the hydroxyl oxygen in the ionization of acetic acid resulted from this definition. It can be seen from Table $V$ that the $\pi$-populations at the two oxygens were about the same in acetic acid and in acetate ion.

Energies of Monocation and Dications. In our previous study of allyl cations and anions, the resonance stabilization of the cations was found to be much more important than that for the anions. ${ }^{5}$ The difference had a simple origin. In allyl cation, the $\pi$-electrons may be distributed one per $\mathrm{C}-\mathrm{C}$ bond, minimizing electron repulsion. In the anion, however, the additional two electrons will result in an increase in electron repulsion that will markedly reduce the delocalization energy.

The energies of the cations derived by removing one ${ }^{18}$ or two hydride ions from isobutene are given in Table VI. For comparison, the energies of guanidine, the guanidinium ion, ${ }^{19}$ and some related compounds were calculated, and these data also are included in the table. In our previous study, the rotational barrier for allyl cation was $34.4 \mathrm{kcal} / \mathrm{mol}$ at the MP3/6-311++G**// 6-31G* level. The barrier for methallyl cation was about the same $(33.3 \mathrm{kcal} / \mathrm{mol})$. We have proposed that these barriers for the allyl cations are composed of about half from loss of resonance stabilization and half from the increase in electrostatic energy as the volume associated with the charge is decreased. ${ }^{5}$

The energy of forming the dication was, as expected, quite high. Of more direct interest, the calculated rotational barrier was found to be only $20 \mathrm{kcal} / \mathrm{mol}$, considerably smaller than that for the monocation. A large part of this barrier must be attributed to the increase in electrostatic energy caused by the localization of charge in the rotated ion. ${ }^{5}$ This suggests that the dication does not have much additional stabilization despite its "Y-conjugation". Rotation of one methylene group would still leave an allyl system, and so there should not be much loss of resonance stabilization.

The electron populations for the monocations and dications are given in Table VII, and the charges derived from the populations are summarized in Figure 4. In methallyl cation, a considerable part of the positive charge was borne by the methyl group, but

[^6]Table V．Electron Populations for Anions and Their Parents， $6-311++\mathrm{G}^{* *}$

| compd | atom | $\mathrm{n}_{\pi}$ | $\mathrm{n}_{\mathrm{T}}$ | $T^{a}$ | compd | atom | $\mathrm{n}_{\pi}$ | $\mathrm{n}_{\mathrm{T}}$ | $T^{a}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| isobutene | $\mathrm{C}_{1}$ | 1.0006 | 5.9700 | 37.7712 | enolate dianion 4 | 0 | 1.8802 | 9.4743 | 75.3970 |
|  | H | 0.0360 | 1.0263 | 0.6311 |  | $\mathrm{C}_{3}$ | 0.6618 | 5.0642 | 37.1732 |
|  | $\mathrm{C}_{2}$ | 0.9356 | 6.0500 | 37.8638 | 11. | $\mathrm{C}_{2}$ | 1.5326 | 6.3937 | 37.6879 |
|  | $\mathrm{C}_{3}$ | 0.9130 | 5.8525 | 37.7176 |  | Ha | 0.1002 | 1.1589 | 0.6514 |
|  | Ha | 0.0274 | 1.0345 | 0.6377 | il．＇11］ | Hb | 0.0964 | 1.1793 | 0.6622 |
|  | Hb | 0.5276 | 1.0382 | 0.6363 |  | sum | 6.0004 | 32.0023 | 190.5732 |
|  | sum | 5.9994 | 31.9994 | 156.1530 |  |  |  |  | （190．5733） |
|  |  |  |  | （156．1534） | acetic acid | $\mathrm{C}(\mathrm{Me})$ | 0.9316 | 5.8490 | 37.7398 |
| methallyl anion 1a | $\mathrm{C}_{1}$ | 0.8356 | 5.8617 | 37.7071 |  | Ha | 0.0244 | 0.9844 | 0.6167 |
|  | Ha | 0.5856 | 1.0833 | 0.6511 | 110 | Hb | 0.4998 | 0.9891 | 0.6142 |
|  | Hb | 0.2256 | 1.0848 | 0.6555 |  | C | 0.4202 | 4.1914 | 36.6610 |
|  | $\mathrm{C}_{2}$ | 0.9442 | 6.0447 | 37.8329 |  | $=0$ | 1.6876 | 9.3458 | $75.6867$ |
|  | $\mathrm{C}_{3}$ | 1.4082 | 6.1750 | 37.6869 |  | O | 1.9274 | 9.2982 | 75.6225 |
|  | Hc | 0.1086 | 1.1284 | 0.6578 |  | H | 0.0094 | 0.3528 | 0.3284 |
|  | Hd | 0.0750 | 1.1183 | 0.6537 |  | sum | 6.0002 | 31.9998 | 227.8835 |
|  | sum | 6.0004 | 32.0029 | 155.4989 |  |  |  |  | （227．8838） |
|  |  |  |  | （155．5001） | acetate anion 5 | $\mathrm{C}(\mathrm{Me})$ | 0.8828 | 5.9076 | 37.7425 |
| methallyl anion 1b | $\mathrm{C}_{1}$ | 0.8954 | 5.8608 | 37.7077 |  | Ha | 0.0292 | 1.0785 | 0.6514 |
|  | Ha | 0.0354 | 1.0874 | 0.6570 | － | Hb | 0.5400 | 1.0778 | 0.6473 |
|  | Hb | 0.5502 | 1.0824 | 0.6525 | 114 | C | 0.4118 | 3.9640 | 36.4920 |
|  | $\mathrm{C}_{2}$ | 0.9166 | 6.0421 | 37.8346 |  | $\mathrm{O}_{1}$ | 1.7926 | 9.4462 | 75.5581 |
|  | $\mathrm{C}_{3}$ | 1.3908 | 6.1805 | 37.6839 |  | $\mathrm{O}_{2}$ | 1.8042 | 9.4511 | 75.5697 |
|  | Ha | 0.0798 | 1.1301 | 0.6579 |  | sum | 6.0006 | 32.0030 | 227.3083 |
|  | Hb | 0.0722 | 1.1185 | 0.6530 |  |  |  |  | （227．3081） |
|  | $\mathrm{C}_{4}$ | 1.3602 | 6.1695 | 37.6893 | acetate dianion 6 | $\mathrm{C}_{1}$ | 1.5526 | 6.4235 | 37.6847 |
|  | Ha | 0.0800 | 1.1263 | 0.6582 |  | H | 0.1008 | 1.1744 | 0.6566 |
|  | Hb | 0.0686 | 1.1177 | 0.6542 155.5008 |  | $\mathrm{C}_{2}$ | 0.4952 | 4.2195 | 36.6247 |
|  | sum | 5.9994 | 31.9977 | $\begin{gathered} 155.5008 \\ (155.5000) \end{gathered}$ | いて | 0 | 1.8750 | 9.5032 | 74.4295 |
| trimethylenemethyl dianion 2 | $\mathrm{C}_{1}$ | 0.8422 | 5.9605 | $\begin{gathered} (155.5000) \\ 37.7313 \end{gathered}$ |  | sum | 5.9994 | 31.9982 | $226.4816$ |
|  | $\mathrm{C}_{2}$ | 1.5228 | 6.3438 | 37.6617 | carbonic acid | C | 0.3628 | 3.3703 | 36.1036 |
|  | H | 0.0982 | 1.1675 | 0.6593 |  | $=0$ | 1.7498 | 9.3716 | 75.7021 |
|  | sum | 5.9998 | 31.9969 | $\begin{gathered} 154.6722 \\ (154.6724) \end{gathered}$ |  | O | 1.9344 | $9.2906$ | 75.6453 |
| acetone | 0 | 1.6036 | 9.2966 | （154．6724） |  | H | 0.0092 | 0.3386 | 0.3213 |
|  | 0 | 1.6036 | 9.2966 | 75.6459 |  | sum | 5.9998 | 32.0003 | $\begin{gathered} 263.7389 \\ (263.7384) \end{gathered}$ |
|  | $\mathrm{C}_{2}$ | 0.4666 | 4.8469 | 37.1023 37.7666 |  |  |  |  |  |
| ＂${ }^{\text {coser }}$ | $\mathrm{C}_{3}$ | 0.9144 | 5.9017 | 37.7666 | bicarbonate anion 7 | C | 0.3744 | 3.4112 | 36.1209 |
| 10 年 | Ha Hb | 0.0240 0.5132 | 0.9899 1.0181 | 0.6176 0.6251 |  | $\mathrm{O}_{1}$$\mathrm{O}_{2}$$\mathrm{O}_{3}$Hsum |  | 9.4591 | 75.5870 |
|  | sum | 5.9998 | 31.9991 | 0.6251 192.0170 |  |  | 1.8172 | 9.4394 | 75.6007 |
|  |  |  |  | （192．0175） |  |  | 0.0130 | 0.4021 | 75.5091 |
| enolate anion 3 | 0 | 1.8198 | 9.4344 | 75.4968 |  |  | 6.0008 | 32.0003 | $\begin{gathered} 263.1796 \\ (263.1790) \end{gathered}$ |
|  | $\mathrm{C}_{2}$ | 1.3576 | 6.1713 | 37.7230 |  |  |  |  |  |
| 11. | Ha | 0.0666 | 1.1003 | 0.6451 | carbonate dianion 8 | C | 0.3552 | 3.4229 | 36.1002 |
| $110$ | Hb | 0.0706 | 1.1304 | 0.6605 |  | $\begin{array}{r} \mathrm{O} \\ \text { sum } \end{array}$ | $\begin{aligned} & 1.8810 \\ & 5.9982 \end{aligned}$ | $\begin{array}{r} 9.5231 \\ 31.9922 \end{array}$ | $\begin{array}{r} 75.4286 \\ 262.3860 \\ (262.3857) \end{array}$ |
|  | $\mathrm{C}_{3}$ | 0.6774 | 5.0152 | $37.1855$ |  |  |  |  |  |
|  | $\mathrm{C}_{4}$ | 0.8808 0.0290 | 5.9059 1.0616 | 37.7370 0.6449 |  |  |  |  |  |
|  | Ha | 0.0290 | 1.0616 | 0.6449 |  |  |  |  |  |
|  | Hb | 0.5496 | 1.0887 | 0.6526 |  |  |  |  |  |
|  | sum | 6.0008 | 31.9965 | $\begin{gathered} 191.3980 \\ (191.3978) \end{gathered}$ |  |  |  |  |  |

${ }^{a}$ The electron populations are given for the $\pi$－system（ $n_{\pi}$ ）and for all the electrons（ $n_{T}$ ）．The kinetic energies（ $T$ ）were corrected for the virial defect found in the RHF calculations and sum to a value close to the negative of the total energy（ $E$ ）．The values of $-E$ are given in parentheses．
its $\pi$－charge was small．The central carbon also bore part of the positive charge，but again its $\pi$－charge was small．The same was true of the dication．

The protonation of guanidine to form guanidinium ion may be examined in the same fashion．In order to have another system for comparison，the energies of propanimine（9）and propan－ iminium ion（10）also were calculated．The protonation of guanidine was calculated to be only $10 \mathrm{kcal} / \mathrm{mol}$ more exothermic than that of propanimine．If guanidinium ion were strongly resonance stabilized，one might reasonably expect a considerably larger difference in energy．Some differences should be expected since guanidinium ion would have its charge spread over three equivalent groups，leading to a lower electrostatic energy than for propaniminium ion．Another indication of the low resonance stabilization of guanidinium ion was the small rotational barrier， $14 \mathrm{kcal} / \mathrm{mol}$ ，which was in good agreement with previous calcu－ lations and experimental observations．${ }^{19}$ Most of the barrier probably resulted from the decrease in the volume over which the charge is distributed when one $\mathrm{NH}_{2}$ group was rotated．${ }^{5}$


Figure 4．Atomic charges and energies derived via numerical integration for the cations and their parents．

The charge distributions for guanidine and guanidinium ion （Table VII and Figure 4）show that the nitrogens do not change

Table VI. Formation of Cations

| compd | 6.31G* | $6.311++\mathrm{G}^{* *}(6 \mathrm{D})$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | RHF | RHF | MP2 | MP3 |
| (a) Energies of Cations and Related Compounds, H |  |  |  |  |
| isobutene | -156.11067 | -156.153 37 | -156.75250 | -156.79463 |
| methallyl cation | -155.23517 | -155.27353 | -155.82468 | -155.86361 |
| methallyl dication | -154.13875 | -154.17476 | -154.65580 | -154.69681 |
| methallyl cation, rot. $90^{\circ}$ | -155.18372 | 155.22343 | -155.76904 | -155.81054 |
| methallyl dication, rot. $90^{\circ}$ | -154.10189 | -154.13847 | -154.62370 | -154.664 67 |
| guanidine | -204.11994 | -204.19418 | -204.87989 | -204.895 91 |
| guanidinium ion | -204.52152 | -204.593 08 | -205.26229 | -205.28405 |
| guanidinium ion, rot. $90^{\circ}$ | -204.49699 | -204.568 84 | -205.24110 | -205.26260 |
| propanimine | -172.11599 | -172.16616 | -172.79448 | -172.82821 |
| propaniminium ion | -172.49752 | -172.548 12 | -173.16184 | -173.20080 |
| $\mathrm{H}^{-}$ | -0.422 44 | -0.48696 | -0.50565 | -0.51070 |
| (b) Energies of lonization, $\mathrm{kcal} / \mathrm{mol}$ |  |  |  |  |
| isobutene $\rightarrow$ methallyl cation | 284.3 | 246.5 | 264.9 | 263.8 |
| methallyl ${ }^{+} \rightarrow$ methallyl dication | 422.9 | 383.9 | 416.2 | 414.9 |
| guanidine $+\mathrm{H}^{+} \rightarrow$ guanidinium cation | 252.0 | 250.3 | 240.0 | 243.6 |
| propanimine $+\mathrm{H}^{+} \rightarrow$ ion | 239.4 | 239.7 | 230.5 | 233.8 |
| (c) Rotational Barriers, $\mathrm{kcal} / \mathrm{mol}$ |  |  |  |  |
| methallyl cation | 32.3 | 31.4 | 34.9 | 33.3 |
| methallyl dication | 23.1 | 22.8 | 20.1 | 20.2 |
| guanidinium ion | 14.1 | 15.2 | 13.3 | 13.5 |

Table VII. Atom Properties of Cations, 6-311++G**

| compd | atom | $\mathrm{n}_{\pi}$ | $\mathrm{n}_{\mathrm{T}}$ | $T^{a}$ |
| :---: | :---: | :---: | :---: | :---: |
| methallyl cation | $\mathrm{C}_{1}$ | 0.9590 | 5.8387 | 37.7066 |
|  | Ha | 0.6296 | 0.9623 | 0.6059 |
|  | Hb | 0.1910 | 0.9747 | 0.6128 |
|  | $\mathrm{C}_{2}$ | 0.9522 | 5.8236 | 37.7447 |
|  | $\mathrm{C}_{3}$ | 0.5152 | 5.9951 | 37.8645 |
|  | Ha | 0.0106 | 0.8515 | 0.5615 |
|  | Hb | 0.0134 | 0.8669 | 0.5695 |
|  | sum | 4.0012 | 30.0010 | $\begin{gathered} 155.2738 \\ (-155.2735) \end{gathered}$ |
| methallyl dication | $\mathrm{C}_{1}$ | 0.2940 | 5.9066 | 37.8009 |
| " | H | 0.0042 | 0.7471 | 0.5114 |
| 11 | $\mathrm{C}_{2}$ | 1.0922 | 5.7952 | 37.7047 |
| $11{ }_{11}{ }^{\text {c-11 }}$ | sum | 1.9994 | 27.9976 | $\begin{gathered} 154.1758 \\ (154.1748) \end{gathered}$ |
| guanidine | C | 0.4996 | 3.9681 | 36.6166 |
|  | $\mathrm{N}_{1}$ | 1.7924 | 8.4047 | 55.1017 |
|  | H | 0.0548 | 0.6607 | 0.4928 |
|  | $\mathrm{N}_{2}$ | 1.6958 | 8.3027 | 55.0697 |
|  | Ha | 0.0332 | 0.5986 | 0.4637 |
|  | Hb | 0.0470 | 0.5923 | 0.4595 |
|  | $\mathrm{N}_{3}$ | 1.7930 | 8.2937 | 55.0724 |
|  | Ha | 0.0390 | 0.5771 | 0.4524 |
|  | Hb | 0.0454 | 0.6033 | 0.4650 |
|  | sum | 6.0002 | 32.0012 | $\begin{gathered} 204.1938 \\ (-204 \end{gathered}$ |
|  | C | 0.4286 | 3.7834 | $\begin{gathered} (-204.1942) \\ 36.4879 \end{gathered}$ |
| guanidinium ion | N | 1.8224 | 8.3860 | 55.2061 |
|  | H | 0.0168 | 0.5091 | 0.4148 |
|  | sum | 5.9966 | 31.9960 | 204.5950 |
|  |  |  |  | (-204.5931) |

${ }^{a} T$ is the kinetic energy. Next to each sum is given the total energy obtained in the RHF calculation.
much in going to the ion, and in fact they were calculated on average to have a larger negative charge in the cation than in the parent. Most of the positive charge in the ion was borne by the hydrogens, resulting in having the charge spread over as large a volume as possible so as to reduce the electrostatic energy. As noted above, the change in the $\pi$-charges on going from guanidine to its ion was a result of the definition of "normal" $\pi$-charges. The nitrogens in both species have about the same $\pi$-electron populations.

Guanidine is considered to be an unusually strong base ( $\mathrm{p} K_{\mathrm{a}}$ 13.6), roughly comparable to hydroxide ion, and the origin of its basicity is commonly ascribed to resonance stabilization of the
guanidinium ion. ${ }^{2}$ If this resonance stabilization is not important, what is the origin of the basicity of guanidine? First, it must be recognized that hydroxyl ion in water is actually a relatively weak base. In the gas phase, hydroxyl ion will abstract a proton from toluene, ${ }^{20}$ but no such reaction occurs in solution. The low basicity of aqueous hydroxide ion results from strong hydrogen bonding to water, stabilizing the ion. Protonation leads to the loss of the stabilization due to hydrogen bonding, and as a result the effective basicity is reduced. The basicity of guanidine probably has a similar origin. Here, it is the conjugate acid that is strongly hydrogen bonded to the solvent. As noted above, the nitrogens bear a negative charge, and the positive charge resides largely at the hydrogens that may be involved in hydrogen bonding. ${ }^{21}$

## Conclusions

The most important conclusion that may be derived from this investigation is that $6 \pi$-electrons do not necessarily lead to $\pi$ electron stabilization. Here we may contrast benzene with the $6-\pi$-electron "Y-conjugated" systems. In the former, the $6 \pi$ electrons may be distributed over $6 \mathrm{C}-\mathrm{C}$ bonds, leading to reduced electron repulsion as compared to $\mathrm{C}-\mathrm{C}$ double bonds that have $2 \pi$-electrons distributed over one $\mathrm{C}-\mathrm{C}$ bond. ${ }^{22}$ The Y dianions and guanidinium ion have $6 \pi$-electrons distributed over three $\mathrm{C}-\mathrm{C}$ or other $\sigma$-bonds, or two per bond. Therefore, there is no opportunity to reduce $\pi$-electron repulsion, and little special stabilization is found.

## Experimental

Calculations. The calculations were carried out using GAUSSIAN- $86^{23}$ with standard basis sets. The integration of the charge density and the kinetic energy was carried out with PROAIMS. ${ }^{24}$

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